Network anomaly detection with the restricted Boltzmann machine

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A B S T R A C T
With the rapid growth and the increasing complexity of network infrastructures and the evolution of attacks, identifying and preventing network abuses is getting more and more strategic to ensure an adequate degree of protection from both external and internal menaces. In this scenario many techniques are emerging for inspecting network traffic and discriminating between anomalous and normal behaviors to detect undesired or suspicious activities. Unfortunately, the concept of normal or abnormal network behavior depends on several factors and its recognition requires the availability of a model aiming at characterizing current behavior, based on a statistical idealization of past events. There are two main challenges when generating the training data needed for effective modeling. First, network traffic is very complex and unpredictable, and second, the model is subject to changes over time, since anomalies are continuously evolving. As attack techniques and patterns change, previously gained information about how to tell them apart from normal traffic may be no longer valid. Thus, a desirable characteristic of an effective model for network anomaly detection is its ability to adapt to change and to generalize its behavior to multiple different network environments. In other words, a self-learning system is needed. This suggests the adoption of machine learning techniques to implement semi-supervised anomaly detection systems where the classifier is trained with “normal” traffic data only, so that knowledge about anomalous behaviors can be constructed and evolve in a dynamic way. For this purpose we explored the effectiveness of a detection approach based on machine learning, using the Discriminative Restricted Boltzmann Machine to combine the expressive power of generative models with good classification accuracy capabilities to infer part of its knowledge from incomplete training data.

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1. Introduction
The main goal of a network anomaly detection system is to discriminate the occurrence of hostile activities from the normal network traffic, and such analysis must be accomplished in a sufficiently flexible and effective way to keep up with the continuously evolving world of cybersecurity where new, previously unknown, anomalies can continuously emerge over time. In doing so, it must either try to model any kind of attack or anomalous event that can affect the network (there are thousands of known ones) or simply construct a sufficiently general model describing the normal traffic.

Such model is usually built on the basis of training data, and used in classifying previously unseen or suspicious events. Classification is the fundamental task in unattended detection, by which the system “learns” to automatically recognize complex traffic patterns, to distinguish between different events based on the corresponding patterns, and to make “intelligent” decisions. Specific machine learning techniques, such as Neural Networks or Support Vector Machines can be used to develop a generalization capability from training data needed to correctly classify future data as normal or abnormal. These resulting approaches can be categorized as generative or discriminative. A generative approach builds a model solely based on normal training examples and evaluates each testing case to see how well it fits the model. A discriminative approach, on the other hand, attempts to learn the distinction between the normal and abnormal classes. Thus, based on the characteristics of training data used to build the model, anomaly detection can be divided into three broad classes [1]:

• Supervised anomaly detection: In this class, a training set containing labeled instances for both the normal and anomalous class is available.
• Semi-supervised anomaly detection: The training here only contains instances for the normal class. Anything that cannot be characterized as normal is thus marked as anomalous.
• Unsupervised anomaly detection: No training set is available nor is it needed.

Obviously, the quality of classification crucially depends on the accurateness and comprehensiveness of the model and hence of
the training data on which the model is built. If a complete set of pre-classified or “labeled” categories of normal (or anomalous) behavior is included in the training set (which can be difficult to achieve and even harder to maintain), all the corresponding (or “matching”) instances will be correctly classified. But if some of such categories are not described in the training data, the corresponding instances may be classified incorrectly. In particular, anomalous events are harder to describe, partly because of their negative definition (a-nomalous literally means non-normal). Anomalous events both appear less frequently than normal events and embrace a huge variety of aspects. In fact, one technique for producing a labeled training set consists in creating anomalies artificially, injecting anomalous events in a stream containing normal data. But the description of anomalies obtained in such a way is forcibly limited to the scope and characteristics of the artificial anomalies used. Labeled anomalous data gathered from operational, “real-world” networks are not readily available, for a number of reasons, including the sheer amount of effort needed to produce such data, and the reluctance of network administrators to divulge data that could compromise the privacy of their clients or exfiltrate privileged information about the internal structure of their networks. The immense amount of data to be potentially examined, combined with their complexity and with the level of expert knowledge that would be needed for the analysis is a strong motivator for making the training process as independent as possible from the availability of labeled anomalous data. Furthermore, these data are generated mainly through human intervention, as soon as the community becomes aware of a new menace and detailed information about the attack dynamics and behavior becomes available. This may require a not negligible time that is clearly unacceptable when real-time or timely response to anomalies is strictly necessary. Consequently, anomaly detection systems should avoid being limited by the knowledge of any predefined set of anomalies and should be able to flexibly recognize/classify any unknown event affecting the network operations according to a self-learning semi-supervised or better unsupervised detection approach, so that the knowledge of traffic behavior on which the model is based can be progressively constructed and dynamically change/evolve over time. However, building and training in situ such a generative self-learning model is a lengthy and costly process. Even when the semi-supervised model is used, the overall result will depend on the completeness of the training data, since it is difficult to represent all the features that normal behavior can have. Thus, in this work we focus on semi-supervised anomaly detection, with a perspective aiming at investigating whether normal traffic behavior (and, conversely, anomalous behavior) shares some inherent similarity that we can use to characterize it. The purpose of this analysis is not to concentrate on a near real-time intrusion detection and reaction system but, in a medium-term perspective, to work towards a better and more adequate description of network traffic, also aiming at being as adaptive as possible. The tool which has been selected for this analysis is the Discriminative Restricted Boltzmann Machine, a network of stochastic neurons behaving according to an energy-based model. These networks couple the ability to express much of the variability of data, given by generative models, with the good classification accuracy derived from discriminative classifiers. The main advantages of this approach are that in line of principle it is not restricted to any specific environment, or a priori knowledge base, and that it can enable the detection of any type of unknown anomalous events, being effective in coping with the so-called zero-day attacks.

In Section 2, related work is reviewed. An introductory summary of classical neural networks, energy-based models, and Boltzmann Machines is the subject of Section 3. The proposed model and its assumptions are detailed in Section 4. Sections 5 and 6 are dedicated to the description of the experiments and the discussion of their results. Section 7 contains some concluding remarks and directions for future research.

2. Related work

Anomaly detection in computer networks is a long-established area, with more than 40 years of evolution [2] and contributions that have explored many approaches [1,3]. In a wider perspective, other researchers have considered the time-dependent connection between events, focusing on the casual relationship between an event and its consequences. For example, the problem of correlating events from different sources to isolate the root cause has been investigated in [4]. The study of effects produced by hidden dynamics has been the object of works based on nonlinear analysis, first targeted to traffic classification [5] and then focused on the specific issue of network anomaly detection [6]. Feature-modeling anomaly detection techniques such as FRAC [7] focus instead on the linkage between individual features and attempt to build predictive models for each feature, based on the others. Features that deviate from this prediction indicate an anomaly. Semi-supervised learning has received attention by the research community recently. Mao et al. [8] have proposed a co-training framework based on multi-view data, semi-supervised learning and active learning. Their method requires user intervention. Chen et al. [9] evaluated the application of spectral graph transduction and Gauss random fields to the detection of unknown attacks. Besides classification, they also proposed a semi-supervised method for clustering. An unsupervised clustering algorithm based on competitive learning neural network is described in [10], where instability is reduced by means of a reward-punishment update rule.

3. Background

3.1. Anomaly detection

From a theoretical point of view our network anomaly detection problem can be formulated as follows [11].

A collection of traffic data measurements is described by a scalar time series \(\{x_t\}_{t=1}^T\) governed by a probability distribution \(p(\cdot)\). Although all these measurements are associated to the occurrence of specific events within the event space \(S\), the correspondence between them may not be known in advance. We are interested in partitioning the event space \(S\) into two subspaces corresponding to the normal and the anomalous network traffic conditions. Also, we need to infer the membership of a particular event in one of the above subspaces starting from the corresponding time series values. To accomplish this task, since the probability distribution \(p\) describing the behavior of the time series is unknown, we can use a mechanism enabling the reconstruction of its volumetric representation from the collection \(\{x_t\}_{t=1}^T\). A general approach to the problem of identifying this representation is based on building a Minimum Volume Set (MVS) characterized by a probability mass \(0 < \beta < 1\) associated to the distribution \(p\) for a volume measure \(\mu\) [12], that is:

\[
G_\beta = \arg \min \{\mu(G) : p(G) \geq \beta, \ G \text{ measurable} \}
\] (1)

In the most of the common cases \(\mu\) can be chosen to be the Lebesgue measure, although such technique extend easily to other measures. The parameter \(\beta\) can be chosen by the user to reflect a desired false alarm rate of \(1-\beta\).

These minimum volumes summarize the regions of greatest probability mass of the distribution \(p\), and are useful for detecting
anomalies and constructing confidence regions. Hence, online evaluation of MVSSs satisfying Eq. (1) inherently allows the identification of the highest density regions where the mass of \( p \) is concentrated. All the points falling outside these regions and the associated events can be declared as anomalous. It can be observed that, if \( p \) is a multivariate Gaussian distribution and \( \mu \) is the Lebesgue measure, then the MVSSs are represented as ellipsoids (see Fig. 1).

The most common available methods for estimating \( G \) come from the use of self-learning systems, whose fundamental solutions can be found in the world of neural networks.

### 3.2. Neural network-based learning models

In many problems of practical interest, the entities to be modeled are complex, with statistical regularities, characteristics, and interactions between them. When modeling such a system as a network of interconnected units, this complexity reflects, in turn, into an intricate mesh of relationships between units. These units can be arranged in a few layers (even one) with many units, or in multiple smaller layers. Theoretical results suggest [13] that functions admitting a compact representation in an architecture with a given number of layers would require a very large number of units in shallower architectures. However, finding the appropriate values for the parameters in these architectures is far more challenging than in the single-layer case, because there is no information about the expected behavior of intermediate layers [14]. In classical neural networks, training algorithms akin to backpropagation only try to model the dependence of the output from the input. Restricted Boltzmann Machines (RBMs), instead, are networks of stochastic neurons that can be trained in a greedy fashion. Deep Belief Networks [15,14] are obtained by stacking RBMs on one another so that the input to one layer is given by the hidden units of the adjacent layer, as if they were data, and adding a last discriminative layer. A hybrid system based on a combination of Support Vector Machines (SVMs) and DBNs has been proposed [16], with a primary focus on feature reduction.

#### 3.2.1. Classical neural networks

The term “neural network” has its origins in attempts to find mathematical representations of information processing in biological systems [17]. Modeling cognitive processes is at the basis of building intelligent information systems capable, to an extent, of activities such as analysis, reasoning, interpretation, and forecasting [18].

Three dimensions are typically needed to describe a neural network:

- **Architecture**: Specifies what variables are involved in the network and their topological relationships, for example, the variables involved in a neural network might be the weights of the connections between the neurons, along with the activities of the neurons.
- **Activity rule**: Most neural network models have short time-scale dynamics: local rules define how the activities of the neurons change in response to each other. Typically the activity rule depends on the weights (the parameters) in the network.
- **Learning rule**: The learning rule specifies the way in which the neural network’s weights change with time. This learning is usually viewed as taking place on a longer time scale than the time scale of the dynamics under the activity rule. Usually the learning rule will depend on the activities of the neurons. It may also depend on target values supplied by a teacher and on the current value of the weights.

The multilayer perceptron is perhaps the simplest specific class of neural network, yet it has proven to be of great practical value. A multilayer feedforward network consists of a set of neurons that are logically arranged in layers. There are at least two layers, the input and output ones. The outputs (activations) of neurons in the input layer are determined by the network’s input. Usually, one or more hidden layers are located between the input and output layers. Data flow in one direction (hence the term feedforward): from the outputs of the previous layer to the inputs of the next layer, so the output of the network is a function of its inputs. The output of such a network can be computed in a single deterministic pass. Every single neuron, represented in Fig. 2 as a circle, has \( n \) inputs \( x = (x_1, \ldots, x_n) \), plus another dummy input always valued at 1, acting as a bias \( b \). Every neuron is characterized by \( n \) weights \( w = (w_1, \ldots, w_n) \) and an activation function \( f \) that is applied to the weighted sum of the inputs, yielding as result:

\[
    f \left( \sum_{i=1}^{n} w_i \cdot x_i + b \right) = f(w^T x + b).
\]

The operational behavior of the network is principally determined by the weights: the exact shape of the activation function only affects the expressive power of the network in a minor way; instead it influences the convergence of the training procedure. The simplest form of nontrivial activation function is the threshold function \( f_{th} = 1 \) if \( x > 0 \) and 0 otherwise. In general, a differentiable activation function is preferred. A common family of activation functions is the sigmoid functions. An example of sigmoid function is the logistic sigmoid:

\[
    \text{sigm}(x) = \frac{1}{1 + e^{-x}}
\]

![Fig. 2. A typical three-layer network, with five inputs, eight hidden units, and two outputs.](image)
whose derivative is always positive and given by the logistic equation

\[
\frac{d}{dx} f(x) = f(x) \cdot (1 - f(x))
\]

Other examples of sigmoid functions are the hyperbolic tangent and the scaled arctangent. Clearly none of these sigmoid functions can reach their respective theoretical bounds, so usually one assumes that a neuron is activated when its output value is about 0.9 and that a neuron is turned off when its output is about 0.1. It is reasonable, instead, to use the extremes as inputs to the network. In the field of neural networks there are very few theoretical strict rules on how to define the architecture of the network. One of these says that all problems that can be solved by a neural network do not require more than two layers. In practice, for the majority of the problems one hidden layer of hidden neurons is enough.

A good method for the determination of the hidden layers is to start with a network with a single hidden and few hidden neurons. If the networks perform poorly, increase the number of hidden neurons. When the number of neurons gets large and the performances of the network do not improve, it can be more productive to introduce a new hidden layer and reduce the total number of hidden neurons. Choosing the right number of neurons for a hidden layer is also not trivial. If there are too few neurons, the network has not enough resources to learn the general features of the training population. Using too many neurons increases the training time, and this not necessarily yields a corresponding increase of performance. In fact, too many neurons can cause over-fitting: the network can capture a large quantity of information not only about important general features, but also specific features of the training set. In passing, one should note that reasoning about the choice of a sensible number of hidden neurons heavily depends on the task the network is designed for: practical rules valid in discriminative tasks are not very sensible to that in Fig. 2. The probability of a state \( P(v, h) \) depends only on the energy of that state \( E(v, h) \), with a Boltzmann distribution function:

\[
P(v, h) = \frac{\exp(-E(v, h))}{\sum_h \exp(-E(v, h))}
\]

where the normalization factor at the denominator is usually denoted by \( Z \) (this comes from Statistical Mechanics, where \( Z \) is termed Partition Function\(^1\)), i.e.,

\[
Z = \sum_v \exp(-E(v, h)).
\]

\( P(v, h) \) is the joint probability of the visible and the hidden variables, that is, the probability of every possible pair of a vector of visible units and a vector of hidden units. Since only the \( v \) are actually observed, we are interested in the marginal distribution \( P(v) \) summing over all configurations of the latent variables:

\[
P(v) = \sum_h P(v, h) = \sum_h \frac{\exp(-E(v, h))}{Z}.
\]

Observing that

\[
Z = \sum_{x,h} \exp(-E(x, h)) = \sum_x \sum_h \exp(-E(x, h)),
\]

Eq. (3) can be transformed into a form similar to Eq. (2) by introducing the notion of Free Energy \( F \):

\[
\exp(-F(x)) = \sum_h \exp(-E(x, h)),
\]

so that

\[
P(x) = \frac{\exp(-F(x))}{\sum_x \exp(-F(x))} = \frac{\sum_h \exp(-E(x, h))}{Z}.
\]

\(^1\) \( Z \) comes from the German word Zustandssumme, sum over states.
To minimize the negative data log-likelihood, its gradient with respect to the parameters of the model, $\theta$, must be considered: 

$$
\frac{\partial \log P(\mathbf{v})}{\partial \theta^n} = \sum_h \left[ \frac{\partial \log P(\mathbf{v}, \mathbf{h})}{\partial \theta^n} - \sum_{\mathbf{v}, \mathbf{h}} P(\mathbf{v}, \mathbf{h}) \frac{\partial \log P(\mathbf{v}, \mathbf{h})}{\partial \theta^n} \right]
$$

where $\mathbb{E}$ denotes the expectation operator. To overcome the difficulty of calculating this gradient analytically (the expectation involves all possible input configurations), Restricted Boltzmann Machines (RBMs) were introduced.

In RBMs, no intra-layer links are allowed [19]. A hidden variable still does influence visible variables (and vice versa) but is not allowed to depend on the value of another hidden variable. The same is true for the visible variables. An RBM can be represented by a network of stochastic binary neurons, whose states are observable, which are connected to stochastic, unobservable, hidden units. Connections are bidirectional. Neurons have two states and will be activated with a probability which is a smooth function of the energy. The function energy of a RBM is

$$
E(\mathbf{v}, \mathbf{h}) = -\mathbf{h}^T \mathbf{W} \mathbf{v} + \mathbf{c}^T \mathbf{h},
$$

(5)

where $\mathbf{h}^T$ is the transpose of $\mathbf{h}$, and $\mathbf{b}$ and $\mathbf{c}$ are the biases, respectively, of the visible and the hidden units. The structure of a RBM, with no intra-layer dependence, allows us to write

$$
p(\mathbf{v} | \mathbf{h}) = \prod_i p(v_i | h_i) \quad \text{and} \quad p(\mathbf{h} | \mathbf{v}) = \prod_j p(h_j | \mathbf{v}).
$$

(6)

The most commonly used case involves binary variables. However, RBMs can be generalized to unrestricted real-valued inputs. With binary units, Eqs. (6) can be rewritten as

$$
P(v_i = 1 | \mathbf{h}) = \text{sigmoid} \left( b_i + \sum_j w_{ij} h_j \right)
$$

and

$$
ptP(h_j = 1 | \mathbf{v}) = \text{sigmoid} \left( c_j + \sum_i w_{ij} v_i \right).
$$

This results in a parametric model of the joint distribution between hidden variables and the observable inputs. The parameters are $\theta = (\mathbf{W}, \mathbf{b}, \mathbf{c})$. Training means finding the values of these parameters that correspond to desirable values for the energy, usually such that the energy is minimized. Thus, a possible training strategy may aim at minimizing the log-likelihood of the training data that is estimating its gradient with respect to the model parameters. While an exact computation is intractable, the gradient can be estimated using a method called contrastive divergence (CD). CD replaces the expectation with a sample taken over a limited number of Gibbs sampling steps. Samples of $p(\mathbf{v})$ can be obtained by running a Markov chain to convergence, by using Gibbs sampling as the transition operator. Visible units are sampled simultaneously, given fixed values of the hidden units (recall that visible units are conditionally independent).

Similarly, hidden units are sampled simultaneously, given the visible variables. At iteration $i$, the hidden units $\mathbf{h}^{(i)}$ are sampled, i.e., chosen at random with probability $\text{sigmoid}(\mathbf{W} \mathbf{v}^{(i-1)} + \mathbf{c})$. This is called positive phase, because it decreases the energy (increases the probability) of training data. Then, the network is allowed to set the values of the visible variables. This also corresponds to random sampling from the distribution of $p(\mathbf{v} | \mathbf{h}^{(i)})$ and is called negative phase, because it increases the energy (decreases the probability) of samples generated by the model. In theory, each parameter update in the learning process would require waiting for convergence of one Markov chain. In practice, after initializing the chain without using a random value but with a training example, even a single step of Gibbs sampling has been shown to yield good results.

Training is obtained by cycling through the training data and updating the parameters with the values obtained by CD multiplied by the learning rate $\lambda$.

3.2.3. Discriminative restricted Boltzmann machines

The discriminative RBM is a promising tool in statistical machine learning [22]. In contrast to the Restricted Boltzmann Machine (RBM), which is a generative classifier aimed at producing a model that describes inputs, capturing as much of their variational potential as possible, the discriminative RBM aims at combining the descriptive power with a sharp classification ability.

In order to make an RBM operate in a supervised fashion, we introduce an additional input containing the targets. The datasets will thus be structured as sequences of pairs $(\mathbf{v}, y)$ comprising an input vector $\mathbf{v}$ and a class $y \in \{1, \ldots, C\}$. It is actually convenient to “vectorize” the class, introducing a vector $\mathbf{y}$ whose $j$-th component is $\delta_{j,y}$, using the Kronecker delta.

In a DRBM, the joint distribution of Eq. (2) becomes then $p(\mathbf{v}, \mathbf{h}, \mathbf{y}) = \exp(-E(\mathbf{v}, \mathbf{h}, \mathbf{y}))$ and the energy of Eq. (5) becomes

$$
E(\mathbf{v}, \mathbf{h}, \mathbf{y}) = -\mathbf{h}^T \mathbf{W} \mathbf{v} - \mathbf{c}^T \mathbf{h} - \mathbf{d}^T \mathbf{y} - \mathbf{h}^T \mathbf{U} \mathbf{y}.
$$

What matters most in a classification task is not a correct joint distribution, but the accuracy for classification. In Discriminative RBMs, we optimize directly $p(\mathbf{y} | \mathbf{v})$ instead of $p(\mathbf{y} | \mathbf{v})$. The loss function will thus be

$$
\ell_{\text{discr}} = \sum_i \log p(y^{(i)} | \mathbf{v}^{(i)})
$$

(7)

and the gradient can be computed exactly

$$
\frac{\partial \log p(y^{(i)} | \mathbf{v}^{(i)})}{\partial \theta} = \sum_j \text{sigmoid}(a_{ij} | \mathbf{v}^{(i)}) \frac{\partial a_{ij} | \mathbf{v}^{(i)}}{\partial \theta} - \sum_j \text{sigmoid}(a_{ij} | \mathbf{v}^{(i)}) \frac{\partial a_{ij} | \mathbf{v}^{(i)}}{\partial \theta}
$$

where $a_{ij} = c_j + \sum_k w_{jk} v_k + U_{ij}$.

As it can be seen, DRBMs have many things in common with feedforward neural networks. The added value of an energy-based machine, such as the one at the basis of RBMs, is that it introduces generative capabilities in an explicit, controllable, way [22].

Whereas the use of binary variables has been previously assumed, RBMs can easily accommodate different variables. For example, units that can assume one state out of $K$ distinct states are dealt with softmax units, whose probability of activation is

$$
P_j = \frac{e^{v_j}}{\sum_k e^{v_k}}
$$

4. DRBM for semi-supervised anomaly detection

Even when we are able to observe anomalous data, it is often difficult or somewhat impossible to identify the anomalous training samples $a priori$. In other words, we must be able to detect anomalies without knowing what they look like. In semi-supervised anomaly detection systems, the classifier is trained with data in the normal class only. In a sense, this presents an interesting analogy with the self-model of the human immune system [23, Chapter 7]. The immune system has indeed inspired a rich line of research in network security (see, for example, [24,25]). To be effective, the immune defenses should be capable to attack
foreign cells. At the same time, attacking all cells indiscriminately would mean bringing harm exactly to the organism (the self) which the immune system is intended to protect (as it happens in autoimmune diseases). Through processes known as positive and negative selection, T-cells lymphocytes are selected in a gland known as thymus so that they react to proteins which are found on all cells of the body (so that body cells are not felt as “too foreign”), but not react too much as to attack them (hence acting against the organism itself). Anything that is not known (not corresponding to the image of self) is labeled as anomalous. Naturally, this does not mean that everything not matching with the model is actually anomalous. Besides the effects of the dynamic, adaptive nature of the network traffic (and of biological systems), the possibility that the model does not completely describe all the instance of normal behavior (a task that can be represented by these systems), the possibility that the model does not completely describe all the instance of normal behavior (a task that can be overwhelmingly difficult and lengthy) should be considered. This approach focuses on understanding the process generating the traffic data, and is very useful to ease the construction of the model of normal or anomalous behavior, since it allows the system to learn about the occurrence of a specific phenomenon via inductive inference based on observing the empirical data that represent incomplete information about the phenomenon itself.

Even though training data includes only normal events, and thus any deviation from such “normality” would trigger an alert, the overall performance of classifiers in this group would not necessarily be remarkable. In fact, the very notion of normality is vague in itself and it is hard to model all the facets that normality can have regardless of the effort that can be put into making the collection of training data as extensive and comprehensive as possible, it is perfectly reasonable that many instances belonging to the normal class show distinctive features that separate them from those found in the training set and thus are flagged as anomalous. Thus, a high number of classification errors can be expected of these systems.

Remark 1. In semi-supervised anomaly detection, classification errors most likely are normal events incorrectly classified as anomalous, i.e., false positives.

It should be noted that false positives, although less harmful than false negatives, are undesirable in the context of anomaly detection. Events flagged as anomalous should be analyzed more closely (perhaps by humans), thus absorbing inordinate amount of resources. Starting from these considerations, some questions immediately arise. Can we do better? Is there some form of “inherent” similarity between all normal traffic? Do all normal traffic flows share some common value ranges for a significant set of features, as well as correlation and sequencing between them? Notably, a recent paper confirms that anomalous traffic has intrinsic properties regarding self-similarity which are different from those of normal traffic [26]. The idea that we intend to test is whether there is a deep similarity between normal behaviors, so that a learning model with high expressive power can describe all the nuisances of normal traffic when comparing it against unseen anomalous traffic. The DRBM, which combines the expressive power of generative models with good classification accuracy, has been selected as a tool to test this hypothesis.

4.1. Assumptions

The following assumptions are taken as valid hereinafter:

- No packet payload is available. There are many reasons for that: to begin with, some data sources that can likely be used for the purpose of this analysis natively do not contain any payload. Typical examples include NetFlow records and Network Address and Port Translation (NAPT) log files [27]. In addition, even if the data source is a packet capture, data can be limited to protocol headers or be truncated to a few bytes. This may happen for privacy concerns (users are very sensitive about the content of their traffic being captured) or simply for the sake of saving storage space.
- It is anticipated that the parameters characterizing a baseline may change over a sufficient long time. Thus, training should be repeated at regular intervals. This theme will be the object of future research and will not be further expanded here.

5. Experiments

A set of experiments was performed by testing the trained network against the processed data from two real-world traces, each one describing all the traffic involving a specific workstation for 24 h. Traffic on one host was normal, while the other one had been infected by a bot [29]. The bot communicated via IRC with other hosts in its botnet. All this traffic was defined as anomalous. This had considerable implications, which will be discussed later. Anomalous connections were flagged manually. The “clean” dataset contains 12,056 connections, while of the 12,317 connection in the second dataset, 4182 were anomalous. The first experiment in this set had the goal of testing the accuracy of the DRBM to recognize anomalous traffic on real data.

Another experiment involved the “cross” use of training and test data: the DRBM was trained with KDD data (using the 10% training KDD dataset), and tested against real data. All tests were repeated 10 times, randomizing the order of the test data.

The KDD 99 dataset is the data set used for the Third International Knowledge Discovery and Data Mining Tools Competition, which was held in conjunction with the Fifth International Conference on Knowledge Discovery and Data Mining (KDD 99). The raw training data amounts to about 4 GB of compressed packet capture data from seven weeks of network traffic. This was processed into 4,898,431 connection records, with a set of 41 features describing various aspects. Similarly, the two weeks of test data yielded 2,984,154 (unlabeled) connection records. A smaller training dataset, containing 10% of the connections (but representative of the anomalies), is also available (Table 1). Each connection is labeled as either normal, or as an attack, with exactly one specific attack type. Each connection record consists of about 100 bytes. Attacks fall into four main categories:

1. **DoS**: denial-of-service, e.g., SYN flood: the attack objective is to prevent legitimate users from accessing a service;
2. **R2L**: unauthorized access from a remote machine, e.g., guessing password: the attack objective is to get access to a machine from outside;
3. **U2R**: unauthorized access to local superuser (root) privileges, e.g., “buffer overflow” attacks: the attack objective is to obtain elevated privileges;
4. **Probe**: reconnaissance and other probing, e.g., port scanning – the attack objective is to gain information about target host or networks.

We have to chose how many features must be used for classification, and how many patterns are needed for each class. In our experiments, we use only part of the total training data, namely, those containing “normal” connections. This leads to 97,278 instances.

Remark 2. While the KDD dataset has been used in a substantial number of research works, it has been heavily criticized [28], as being excessively “artificial”, in the sense that normal traffic into

\[ \text{http://www.sigkdd.org/kddcup/index.php?section=1999} \]
which anomalies were injected does not resemble real traffic; this may add an undesired bias to the data, weakening the results deriving from experiments upon them.

5.1. Features

In order to construct the needed traffic measurement space, we have to determine a basic set of features describing the traffic pattern in a specific time interval (the observation epoch). Let \( F \) denote the feature space describing the network traffic. We use a multi-dimensional feature vector \( \mathbf{f} \in F \) built from the fundamental traffic observations (e.g., the overall byte rate or the average packet inter-arrival time) by computing on each epoch some traffic behavior discriminators.

The number of traffic features that can be simultaneously evaluated introduces great control granularity in the detection process by adding multiple points of observation, and hence new dimensions in the decision space that can ease correlation and inference activities in the DRBM-based binary classification process. Having multiple different observations associated to the individual traffic components may also be helpful in spotting and describing the nature and behavior of the observed anomalous phenomena (e.g., protocols affected, transport facilities used, traffic volumes distribution). This last issue can be of fundamental importance in the development of countermeasures or reaction strategies that can be a very interesting subject for further research.

In the experiments, 28 out of 41 features were used, namely, those related to network traffic. These features are listed in Table 2.

Most features take a value in a numerical range, and are indicated as “continuous”. Other features are nominal, i.e., they assume one value from a discrete set of possible values. These features are tagged as “discrete”. Note that some features are derived, i.e., calculated starting from the values of other features. Features can be lumped into three groups: the first group (lines 1–7 of Table 2) includes basic features of individual TCP connections; the second group (lines 8–18 of Table 2) includes time-based features computed over a two-second interval a set of counters for connection having specific characteristics; the third group (lines 19–28 of Table 2) includes derived host-based features, which were computed using, instead of a time window, a window of 100 connections to the same host. Within the second group, the “same host” features examine only the connections in the past 2 s that have the same destination host as the current connection, and calculate statistics related to protocol, service or behavior. The similar “same service” features examine only the connections in the past 2 s that have the same service as the current connection.

5.2. Preprocessing

A preprocessing step was needed to transform the packet traces into a connection-based format such as the one used in the KDD dataset. For this purpose, the bro IDS\(^4\) has been used, together with a properly crafted trace parsing tool. bro is a powerful network monitoring framework, originally developed by Vern Paxson at the International Computer Science Institute and the National Center for Supercomputing Applications, that, while focusing on network security issues, provides a comprehensive platform for more general network traffic analysis. After processing the traffic traces with bro, a further step, encoding the nominal traffic features with arbitrary numeric values (tokens), is performed. For example, the protocol_type (e.g., tcp) is encoded by using the IANA-assigned protocol numbers, and so on.

A forest structure has been used in parsing the connection data from bro to make the preprocessing phase more efficient. During the tokenization, two search trees are built, structured according to the scheme reported in Fig. 3. There are three types of node: source-Ip, destination-Ip, destination-Port. Each path within a tree identifies a connection. A set of counters \( C = [c_1, \ldots, c_n] \) (with \( n = |C| \)) is associated to each node: for instance, if there are \( n \) connections from the source IP 192.168.0.1, the connection counter in the 192.168.0.1-node will have value \( 5 \). It is trivial to note that the sum of the counters \( c_i \) associated to the children of a particular node is equal to the corresponding counter \( c_i \) on the node itself. When a new connection is found in the traffic trace, the respective path is added, but if the first part of the path is already in the tree, only the second one is added to it, and the counters of the first one are simply incremented. In this way, the value of the traffic features for each connection can be computed in a straightforward way.

For instance, the feature count is the number of connections to the same host (during the current connection in the past 2 s), so to compute this feature, the only thing to do is to read the value of the specific counter in the destination node of the path from source to destination. Another forest with a specular structure (i.e., with paths going from nodes describing the destination to nodes describing the source) is needed, because most features, to be computed, need the destination-IP as the search base. For instance if we want to know the number of connections from a specific host, say X, to a destination Y, using the destination-IP tree, the only thing to do is to read the associated counter value in the node X, chosen between the sons of Y. With this approach, it is possible to compute all the needed features: some of them are equal to the values of specific counters in the tree nodes, but other ones can be easily derived from them, like the percentage of connections that were reset or the connections with SYN errors (e.g., these connections will have status S0 in bro).

5.3. Methodology

The success of a classifier meant to be used in practice depends ultimately on its ability to perform well not only with the data used for its testing, but most of all with real-world data. Although a methodologically sound procedure ensures that the classifier is tested against data it has never seen before (i.e., in the training phase), there is no guarantee whatsoever that testing data will be representative of, and resemble closely, real-world data. Such data surely are not available at the time of testing. On the other hand, when using a portion of the training data as a validation dataset to verify and refine the selection of model hyper-parameters, training data could “leak” some information about the validation conditions if the partitioning of data into training and validation sets is not done properly so as to ensure that instances relative to the same (or very close) conditions go in the same part. Connections recorded with the same conditions might, in fact, share some

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\(^4\) http://www.bro-ids.org/
similarity that might unnoticeably cause over-fitting when two instances taken in the same day are used both in the training and validation sets. The classification accuracy would thus be overestimated. Connection that are comparable in terms of amount of data being exchanged might be too similar to one another for the validation to avoid biasing. Thus, a check that has been added is to subdivide connections into categories based on data volume, and to ensure that all the connections belonging to the same category are used either as training or as validation inputs.

5.4. Evaluation criteria

The performances of a network must be evaluated by testing it on a different data set than the one on which it was trained. The relatively large number of parameters involved (all the weights) means that it is too easy for the network to acquire unique characteristic of the training set (over-fitting), rather than generalizing on properties of the population. While the mean square error is easy to compute, its most obvious disadvantage is that it is a purely mathematical construct, which may have little meaning with respect to the practical task performed by the network. If the task is to classify a pattern into one of the several categories, the mean square error tells us nothing about expected frequency of misclassification. A more important problem with the MSE as a guide to performance is that it fails to distinguish minor and serious errors. If the task of the network is to classify cases into one of the several categories, examining a confusion matrix can be highly informative. A confusion matrix is a matrix containing as many rows and columns as there are classes. For every case, its class is chosen to be that corresponding to the output neuron that has the maximum activation. The content of the entry at the i-th row and the j-th column of the confusion matrix is the number of test cases that truly belong to class i but which were classified into class j. Ideally, one would obtain a strictly diagonal matrix. Quantities in off-diagonal positions represent misclassifications. The principal strength of the confusion matrix is that it clearly identifies the nature of errors, as well as their quantity. The experimenter is then free to evaluate the performances of the

Table 2 Features used in the experiments.

<table>
<thead>
<tr>
<th>No.</th>
<th>Feature name</th>
<th>Description</th>
<th>Data type</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>duration</td>
<td>Length (number of seconds) of the connection</td>
<td>continuous</td>
</tr>
<tr>
<td>2</td>
<td>protocol_type</td>
<td>Type of the protocol, e.g., tcp or udp</td>
<td>discrete</td>
</tr>
<tr>
<td>3</td>
<td>service</td>
<td>Network service on the destination, e.g., http or telnet</td>
<td>discrete</td>
</tr>
<tr>
<td>4</td>
<td>flag</td>
<td>Normal or error status of the connection</td>
<td>discrete</td>
</tr>
<tr>
<td>5</td>
<td>src_bytes</td>
<td>Number of data bytes from source to destination</td>
<td>continuous</td>
</tr>
<tr>
<td>6</td>
<td>dst_bytes</td>
<td>Number of data bytes from destination to source</td>
<td>continuous</td>
</tr>
<tr>
<td>7</td>
<td>land</td>
<td>1 if connection is from/to the same host/port; 0 otherwise</td>
<td>discrete</td>
</tr>
<tr>
<td>8</td>
<td>wrong_fragment</td>
<td>Number of “wrong” fragments</td>
<td>continuous</td>
</tr>
<tr>
<td>9</td>
<td>urgent</td>
<td>Number of urgent packets</td>
<td>continuous</td>
</tr>
<tr>
<td>10</td>
<td>count</td>
<td>Number of connections to the same host as the current connection in the past two seconds</td>
<td>continuous</td>
</tr>
<tr>
<td>11</td>
<td>srv_count</td>
<td>Number of connections to the same service as the current connection in the past two seconds</td>
<td>continuous</td>
</tr>
<tr>
<td>12</td>
<td>serror_rate</td>
<td>% of same-host connections that have “SYN” errors</td>
<td>continuous</td>
</tr>
<tr>
<td>13</td>
<td>srv_serror_rate</td>
<td>% of same-service connections that have “SYN” errors</td>
<td>continuous</td>
</tr>
<tr>
<td>14</td>
<td>error_rate</td>
<td>% of same-host connections that have “REJ” errors</td>
<td>continuous</td>
</tr>
<tr>
<td>15</td>
<td>srv_rerror_rate</td>
<td>% of same-service connections that have “REJ” errors</td>
<td>continuous</td>
</tr>
<tr>
<td>16</td>
<td>same_srv_rate</td>
<td>% of same-host connections to the same service</td>
<td>continuous</td>
</tr>
<tr>
<td>17</td>
<td>diff_srv_rate</td>
<td>% of same-host connections to different services</td>
<td>continuous</td>
</tr>
<tr>
<td>18</td>
<td>srv_diff_host_rate</td>
<td>% of same-service connections to different hosts</td>
<td>continuous</td>
</tr>
<tr>
<td>19</td>
<td>dst_host_count</td>
<td>Count of connections having the same destination host</td>
<td>continuous</td>
</tr>
<tr>
<td>20</td>
<td>dst_host_srv_count</td>
<td>Count of connections having the same destination host and using the same service</td>
<td>continuous</td>
</tr>
<tr>
<td>21</td>
<td>dst_host_same_srv_rate</td>
<td>% of connections having the same destination host and using the same service</td>
<td>continuous</td>
</tr>
<tr>
<td>22</td>
<td>dst_host_diff_srv_rate</td>
<td>% of different services on the current host</td>
<td>continuous</td>
</tr>
<tr>
<td>23</td>
<td>dst_host_same_src_port_rate</td>
<td>% of connections to the current host having the same src port</td>
<td>continuous</td>
</tr>
<tr>
<td>24</td>
<td>dst_host_srv_diff_host_rate</td>
<td>% of connections to the same service coming from different hosts</td>
<td>continuous</td>
</tr>
<tr>
<td>25</td>
<td>dst_host_serror_rate</td>
<td>% of connections to the current host that have an S0 error</td>
<td>continuous</td>
</tr>
<tr>
<td>26</td>
<td>dst_host_srv_serror_rate</td>
<td>% of connections to the current host and specified service that have an S0 error</td>
<td>continuous</td>
</tr>
<tr>
<td>27</td>
<td>dst_host_rerror_rate</td>
<td>% of connections to the current host that have an RST error</td>
<td>continuous</td>
</tr>
<tr>
<td>28</td>
<td>dst_host_srv_rerror_rate</td>
<td>% of connections to the current host and specified service that have an RST error</td>
<td>continuous</td>
</tr>
</tbody>
</table>

Fig. 3. Tree-like structure for the efficient computation of features.
network in terms of relative severity of misclassifications. The evaluation parameters that have been selected are thus:

- **Accuracy**: Is the reliability of the rule, usually represented by the proportion of correct classifications, although it may be that some errors are more serious than others, and it may be important to control the error rate for some key class.
- **Speed**: In some circumstances, the speed of the classifier is a major issue. A classifier that is 90% accurate may be preferred over one that is 95% accurate if the former is 100 times faster in testing (and such differences in time-scales are not uncommon in neural networks). Such considerations would be even more important when the number of samples to be processed is very large.
- **Comprehensibility**: If it is a human operator who must apply the classification procedure, the procedure must be easily understood, else mistakes will be made in applying the rule. It is important, also, that human operators believe and trust the system. An oft-quoted example is the Three-Mile Island case, where the automatic devices correctly recommended a shutdown, but this recommendation was not acted upon by the human operators who did not believe that the recommendation was well founded.
- **Time to learn**: Especially in a rapidly changing environment, it may be necessary to learn a classification rule quickly, or make adjustments to an existing rule in real time. ‘Quickly’ might imply also that we need only a small number of observations to establish our rule. In addition, retraining can be performed quickly, and this in turn allows it to be performed more often, and our results in Section 6 show that this may very frequently be the case.

### 5.5. Early stopping

Early stopping is a technique to concentrate training efforts. Typically it involves partitioning the data set into three parts: training, validation and testing. Gradient descent on the objective function is performed with data in the training set. In parallel, the resulting model is tested against the validation set (not the testing set) to see how well it is performing in unseen data. Samples in the validation set can be used during training, because they would not be included in the testing set. The training-validation partitioning can also be done in a similar way to that done in n-fold cross validation. The reconstruction error should normally decay steeply at the beginning of training, and then ‘stabilize’ as the effects of noise in the gradient calculations begin to appear. Thus, when accuracy ceases to improve, or starts dropping, optimization is stopped.

### 5.6. Choice of hyper-parameters

In the training phase of Experiment 1, normal traffic of the first real trace was used for training, and traffic from the second trace for testing. The same testing set has been used in Experiment 2. However, in Experiment 2, KDD data purified from attacks were used as training data. Thus, the neural network was allowed to recognize a set of instances of normal traffic. The learning rate has been set to 0.1, while the number of training epochs was initially chosen as 15, trying also 10 and 5. A range of different values were used for the other hyper-parameters. The values obtained with the best 10 combinations have been used for the charts.

### 6. Results

In Fig. 4, the free energy of the RBM is shown for both normal and anomalous connections in the real data set. As it can be observed, the free energy of normal connections tends to oscillate between two intervals. Anomalous behavior, instead, shows two distinctive characteristics. Its free energy reaches extreme values (the positive and negative spikes) or it stays very stably in a narrow interval. The second characteristic can be traced back to routine communication between the malware and its controlling nodes. While the free energy for this activity lies in the range of the free energies associated to normal traffic, values in the specific interval for anomalous traffic are rarely found in normal traffic. The spikes are instead associated with actual commands sent out to the malware agent and to the return of a quantity of data gathered on the infected PC and sent back to a different (possibly up the chain of command) node.

The training times were significant. Training in Experiment 1 over 15 epochs took 186.4 h on a HP DL380 G3.

In Fig. 5, the accuracies obtained for the various experiments are reported. The graphs use boxplot format of Tukey and Chambers and illustrate the distribution of data. The central box is bounded by the first and third quartiles, and thus it encloses the middle 50% of the data. The “whiskers” extend to the minimum and maximum values. A “+” sign indicates the mean, whereas the
horizontal line across the box is drawn at the median. Each box is relative to an experiment. The first (rr) gives the results for the experiment where the DBRM was trained and tested on the real data and the rightmost (kr) the experiment where the DBRM was trained on the KDD dataset and tested on the real data. Recall that data and the rightmost (kr) the experiment where the DBRM was placed on a test set of real traffic.

Thus, artiﬁcial trafﬁc can be affected by unpredictable network noise phenomena. We may overestimate or underestimate anomalous phenomena. Hence, in future applications, to enhance the performance of the classiﬁcation accuracy, a baseline of normal trafﬁc should deﬁnitely be isolated speciﬁcally for the network where the analysis is to be performed.

7. Conclusions

In this paper, the Discriminative Restricted Boltzmann Machine, a recently proposed classiﬁer based on the family of energy-based models, has been applied to network anomaly detection in a semi-supervised fashion. In particular we were interested in decoupling the training data from the testing scenario to assess the generalization abilities of neural networks. The DRBM has been chosen for its ability to combine generative and classiﬁcation power, to capture the inherent aspects of the normal trafﬁc class, and classiﬁcation accuracy.

Experiments conﬁrm that, when the classiﬁer is tested in a network widely different from the one where training data were taken from, the performance suffers. This suggests the need for further investigation over the nature of abnormal trafﬁc and the intrinsic differences with normal trafﬁc.

We can consider that the nonparametric nature of the above techniques can simultaneously become their main strength and Achilles' heel: a nonparametric method is not based on any known form or distribution of the sample observations and consequently it is more robust. At the same time being nonparametric means that no prior knowledge about anomalous phenomena is available to be incorporated into the detection model, greatly reducing its effectiveness. This implies that, since the detection capability is directly associated with the correctness of the underlying self-learned trafﬁc model, if the training set does not accurately represent the real network normal trafﬁc (i.e., it is not realistic), we may overestimate or underestimate anomalous phenomena. Thus, artiﬁcial trafﬁc models are error prone and should not be used for effective semi-supervised training purposes. However, also real trafﬁc patterns used for characterizing the normal behavior can be affected by unpredictable network noise phenomena largely due to the randomness and burstiness of the trafﬁc behavior that can adversely affect the anomaly detection accuracy. Hence, in future applications, to enhance the performance of the detection phase we will try to improve the overall “signal-to-noise ratio” through signal pre-processing by limiting the inﬂuence of the “noisy” components and unwanted dependencies according to some de-noising techniques such as nonparametric regression or other available ones. Directions for future research also include the analysis of feature-modeling detectors, combined with the study of the discriminatory power of single features.

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References


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